

## Disproving Identities

In section 8.3, the textbook gives a number of examples showing how to establish an identity. Recall that an equation  $f(x) = g(x)$  is an identity if it is true for *all* values of  $x$  for which both functions  $f$  and  $g$  are defined. Thus, such an equation is *not* an identity if there is at least one value of  $x$  for which  $f(x) \neq g(x)$ .

Therefore, to disprove a proposed identity  $f(x) = g(x)$ , it is enough to find one value of  $x$  for which the equation is false. This can usually be done fairly easily with a little trial and error.

**EXAMPLE:** Consider the equation  $\cos^2 x - \sin^2 x = 1$ . This equation is actually true at some values of  $x$ , for example at  $x = 0, \pi, 2\pi, \dots$ . However, the equation is false at most values of  $x$ . For example, at  $x = \pi/2$ , the left side is  $-1$  and the right side is of course  $1$ . Since  $-1 \neq 1$ , this is a false identity. Many other choices of  $x$  could also be used to disprove this false identity.